

Do not write on this test. Record all answers on the bubble sheet. **Closed book. No notes.** Work strictly from memory. **No calculators. Scratch paper okay.**

1/2p. Give a tight big-oh  $\Theta()$  bound on the running time  $T(n)$  of this program.

Assume `atoi`, `simpleStatement`, and `simpleCompare` each run in  $\Theta(1)$  time.

- (A)  $n^9$  (C)  $n^7$  (E)  $n^5$  (G)  $n^3$  (I)  $n$   
(B)  $n^8$  (D)  $n^6$  (F)  $n^4$  (H)  $n^2$  (J) 1

```
int main ( int argc, char * * argv ) {
    int n = atoi(argv[1]);
    for ( j = n ; j > 1 ; j-- ) {
        if ( simpleCompare ) {
            if ( simpleCompare ) {
                if ( simpleCompare ) {
                    simpleStatement;
                } else {
                    simpleStatement;
                }
            } else {
                simpleStatement;
            }
        }
    }
    return 0; }
```

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2/2p. Give a tight big-oh  $\Theta()$  bound on the running time  $T(n)$  of this program.

Assume `atoi`, `simpleStatement`, and `simpleCompare` each run in  $\Theta(1)$  time.

- (A)  $n^9$  (C)  $n^7$  (E)  $n^5$  (G)  $n^3$  (I)  $n$   
(B)  $n^8$  (D)  $n^6$  (F)  $n^4$  (H)  $n^2$  (J) 1

```
int main ( int argc, char * * argv ) {
    int n = atoi(argv[1]);
    if ( simpleCompare ) {
        if ( simpleCompare ) {
            if ( simpleCompare ) {
                simpleStatement;
            } else {
                simpleStatement;
            }
        } else {
            simpleStatement;
        }
    } else {
        if ( simpleCompare ) {
            simpleStatement;
        } else {
            simpleStatement;
        }
    }
    return 0; }
```

---

- 3/2p. Give a tight big-oh  $\Theta()$  bound on the running time  $T(n)$  of this program.  
 Assume `atoi`, `simpleStatement`, and `simpleCompare` each run in  $\Theta(1)$  time.  
 (A)  $n^9$  (C)  $n^7$  (E)  $n^5$  (G)  $n^3$  (I)  $n$   
 (B)  $n^8$  (D)  $n^6$  (F)  $n^4$  (H)  $n^2$  (J) 1

```
int main ( int argc, char * * argv ) {
    int n = atoi(argv[1]);
    for ( g = 1 ; g < n ; g++ ) {
        if ( simpleCompare ) {
            if ( simpleCompare ) {
                if ( simpleCompare ) {
                    simpleStatement;
                } else {
                    simpleStatement;
                }
            }
        } else {
            for ( c = 1 ; c < n ; c++ ) {
                simpleStatement;
            }
        }
    }
    return 0; }
```

- 4/2p. Give a tight big-oh  $\Theta()$  bound on the running time  $T(n)$  of this program.  
 Assume `atoi`, `simpleStatement`, and `simpleCompare` each run in  $\Theta(1)$  time.  
 (A)  $n^9$  (C)  $n^7$  (E)  $n^5$  (G)  $n^3$  (I)  $n$   
 (B)  $n^8$  (D)  $n^6$  (F)  $n^4$  (H)  $n^2$  (J) 1

```
int main ( int argc, char * * argv ) {
    int n = atoi(argv[1]);
    h = n; while ( h > 1 ) {
        if ( simpleCompare ) {
            if ( simpleCompare ) {
                if ( simpleCompare ) {
                    if ( simpleCompare ) {
                        simpleStatement;
                    }
                }
            }
        } else {
            if ( simpleCompare ) {
                simpleStatement;
            } else {
                simpleStatement;
            }
        }
    }
    h -= 10; }
    return 0; }
```

- 5/2p. Give a tight big-oh  $\Theta()$  bound on the running time  $T(n)$  of this program.  
 Assume `atoi`, `simpleStatement`, and `simpleCompare` each run in  $\Theta(1)$  time.  
 (A)  $n^9$  (C)  $n^7$  (E)  $n^5$  (G)  $n^3$  (I)  $n$   
 (B)  $n^8$  (D)  $n^6$  (F)  $n^4$  (H)  $n^2$  (J) 1

```
int main ( int argc, char * * argv ) {
  int n = atoi(argv[1]);
  if ( simpleCompare ) {
    if ( simpleCompare ) {
      j = n; do {
        simpleStatement;
      } while ( j > 1 );
    }
  } else {
    f = 1; while ( f < n ) {
      simpleStatement;
      f++; }
  }
  return 0; }
```

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- 6/2p. Give a tight big-oh  $\Theta()$  bound on the running time  $T(n)$  of this program.  
 Assume `atoi`, `simpleStatement`, and `simpleCompare` each run in  $\Theta(1)$  time.  
 (A)  $n^9$  (C)  $n^7$  (E)  $n^5$  (G)  $n^3$  (I)  $n$   
 (B)  $n^8$  (D)  $n^6$  (F)  $n^4$  (H)  $n^2$  (J) 1

```
int main ( int argc, char * * argv ) {
  int n = atoi(argv[1]);
  if ( simpleCompare ) {
    if ( simpleCompare ) {
      if ( simpleCompare ) {
        if ( simpleCompare ) {
          for ( k = n ; k > 1 ; k -= 10 ) {
            simpleStatement;
          }
        } else {
          simpleStatement;
        }
      } else {
        simpleStatement;
      }
    } else {
      if ( simpleCompare ) {
        simpleStatement;
      } else {
        simpleStatement;
      }
    }
  }
  return 0; }
```

7/2p. Give a tight big-oh  $\Theta()$  bound on the running time  $T(n)$  of this program.

Assume `atoi`, `simpleStatement`, and `simpleCompare` each run in  $\Theta(1)$  time.

(A)  $n^9$  (C)  $n^7$  (E)  $n^5$  (G)  $n^3$  (I)  $n$

(B)  $n^8$  (D)  $n^6$  (F)  $n^4$  (H)  $n^2$  (J) 1

```
int main ( int argc, char * * argv ) {
    int n = atoi(argv[1]);
    e = 1; do {
        for ( b = n ; b > 1 ; b -= 2 ) {
            c = n; while ( c > 1 ) {
                if ( simpleCompare ) {
                    for ( h = 1 ; h < n ; h++ ) {
                        simpleStatement;
                    }
                } else {
                    simpleStatement;
                }
            }
            c -= 3; }
        }
    e++; } while ( e < n );
return 0; }
```

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8/2p. Give a tight big-oh  $\Theta()$  bound on the running time  $T(n)$  of this program.

Assume `atoi`, `simpleStatement`, and `simpleCompare` each run in  $\Theta(1)$  time.

(A)  $n^9$  (C)  $n^7$  (E)  $n^5$  (G)  $n^3$  (I)  $n$

(B)  $n^8$  (D)  $n^6$  (F)  $n^4$  (H)  $n^2$  (J) 1

```
int main ( int argc, char * * argv ) {
    int n = atoi(argv[1]);
    k = 1; while ( k < n ) {
        if ( simpleCompare ) {
            if ( simpleCompare ) {
                for ( f = 1 ; f < n ; f++ ) {
                    for ( a = 1 ; a < n ; a += 10 ) {
                        simpleStatement;
                    }
                }
            }
        } else {
            d = n; do {
                if ( simpleCompare ) {
                    simpleStatement;
                } else {
                    simpleStatement;
                }
            } while ( d > 1 );
        }
        k++; }
return 0; }
```

9/2p. Give a tight big-oh  $\Theta()$  bound on the running time  $T(n)$  of this program.  
Assume `atoi`, `simpleStatement`, and `simpleCompare` each run in  $\Theta(1)$  time.

- (A)  $n^9$  (C)  $n^7$  (E)  $n^5$  (G)  $n^3$  (I)  $n$   
(B)  $n^8$  (D)  $n^6$  (F)  $n^4$  (H)  $n^2$  (J) 1

```
int main ( int argc, char * * argv ) {
    int n = atoi(argv[1]);
    for ( e = n ; e > 1 ; e -= 5 ) {
        if ( simpleCompare ) {
            if ( simpleCompare ) {
                if ( simpleCompare ) {
                    for ( a = n ; a > 1 ; a-- ) {
                        j = 1; while ( j < n ) {
                            simpleStatement;
                            j++; }
                    }
                } else {
                    simpleStatement;
                }
            } else {
                if ( simpleCompare ) {
                    simpleStatement;
                } else {
                    simpleStatement;
                }
            }
        } else {
            if ( simpleCompare ) {
                if ( simpleCompare ) {
                    f = n; while ( f > 1 ) {
                        simpleStatement;
                        f -= 3; }
                    } else {
                        simpleStatement;
                    }
                } else {
                    if ( simpleCompare ) {
                        simpleStatement;
                    } else {
                        simpleStatement;
                    }
                }
            }
        }
    }
    return 0; }
```

- 10/2p. Give a tight big-oh  $\Theta()$  bound on the running time  $T(n)$  of this program.  
 Assume `atoi`, `simpleStatement`, and `simpleCompare` each run in  $\Theta(1)$  time.
- (A)  $n^9$  (C)  $n^7$  (E)  $n^5$  (G)  $n^3$  (I)  $n$   
 (B)  $n^8$  (D)  $n^6$  (F)  $n^4$  (H)  $n^2$  (J) 1

```
int main ( int argc, char * * argv ) {
  int n = atoi(argv[1]);
  for ( j = n ; j > 1 ; j-- ) {
    if ( simpleCompare ) {
      if ( simpleCompare ) {
        for ( i = n ; i > 1 ; i -= 5 ) {
          for ( d = 1 ; d < n ; d++ ) {
            if ( simpleCompare ) {
              for ( e = n ; e > 1 ; e-- ) {
                simpleStatement;
              }
            } else {
              simpleStatement;
            }
          }
        }
      } else {
        if ( simpleCompare ) {
          for ( f = n ; f > 1 ; f -= 5 ) {
            simpleStatement;
          }
        } else {
          simpleStatement;
        }
      }
    } else {
      for ( g = 1 ; g < n ; g += 3 ) {
        if ( simpleCompare ) {
          if ( simpleCompare ) {
            a = 1; while ( a < n ) {
              b = 1; do {
                simpleStatement;
                b += 10; } while ( b < n );
              a++; }
          } else {
            c = 1; do {
              simpleStatement;
              c += 10; } while ( c < n );
            }
          }
        }
      }
    }
  }
  return 0; }
```

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Total points 20.

**Answer Key** (points per line)

1 (2).	I ( $n$ )
2 (2).	J (1)
3 (2).	H ( $n^2$ )
4 (2).	I ( $n$ )
5 (2).	I ( $n$ )
6 (2).	I ( $n$ )
7 (2).	F ( $n^4$ )
8 (2).	G ( $n^3$ )
9 (2).	G ( $n^3$ )
10 (2).	F ( $n^4$ )

Total points 20.