

Do not write on this test. Record all answers on the bubble sheet. **Closed book. No notes.** Work strictly from memory. **No calculators. Scratch paper okay.**

1/2p. Give a tight big-oh  $\Theta()$  bound on the running time  $T(n)$  of this program.

Assume `atoi`, `simpleStatement`, and `simpleCompare` each run in  $\Theta(1)$  time.

- (A)  $n^9$  (C)  $n^7$  (E)  $n^5$  (G)  $n^3$  (I)  $n$   
 (B)  $n^8$  (D)  $n^6$  (F)  $n^4$  (H)  $n^2$  (J) 1

```
int main ( int argc, char * * argv ) {
    int n = atoi(argv[1]);
    b = n; while ( b > 1 ) {
        if ( simpleCompare ) {
            if ( simpleCompare ) {
                for ( a = 1 ; a < n ; a += 10 ) {
                    if ( simpleCompare ) {
                        for ( j = n ; j > 1 ; j-- ) {
                            simpleStatement;
                        }
                    } else {
                        simpleStatement;
                    }
                }
            }
        }
        b--; }
    return 0; }
```

2/2p. Give a tight big-oh  $\Theta()$  bound on the running time  $T(n)$  of this program.

Assume `atoi`, `simpleStatement`, and `simpleCompare` each run in  $\Theta(1)$  time.

- (A)  $n^9$  (C)  $n^7$  (E)  $n^5$  (G)  $n^3$  (I)  $n$   
 (B)  $n^8$  (D)  $n^6$  (F)  $n^4$  (H)  $n^2$  (J) 1

```
int main ( int argc, char * * argv ) {
    int n = atoi(argv[1]);
    for ( i = n ; i > 1 ; i -= 10 ) {
        if ( simpleCompare ) {
            h = 1; do {
                if ( simpleCompare ) {
                    simpleStatement;
                } else {
                    simpleStatement;
                }
                h++; } while ( h < n );
        } else {
            if ( simpleCompare ) {
                simpleStatement;
            }
        }
    }
    return 0; }
```

3/2p. Give a tight big-oh  $\Theta()$  bound on the running time  $T(n)$  of this program.

Assume `atoi`, `simpleStatement`, and `simpleCompare` each run in  $\Theta(1)$  time.

(A)  $n^9$  (C)  $n^7$  (E)  $n^5$  (G)  $n^3$  (I)  $n$

(B)  $n^8$  (D)  $n^6$  (F)  $n^4$  (H)  $n^2$  (J) 1

```
int main ( int argc, char * * argv ) {
    int n = atoi(argv[1]);
    if ( simpleCompare ) {
        if ( simpleCompare ) {
            if ( simpleCompare ) {
                if ( simpleCompare ) {
                    f = n; while ( f > 1 ) {
                        simpleStatement;
                        f--; }
                }
            }
        }
    }
    return 0; }
```

4/2p. Give a tight big-oh  $\Theta()$  bound on the running time  $T(n)$  of this program.

Assume `atoi`, `simpleStatement`, and `simpleCompare` each run in  $\Theta(1)$  time.

(A)  $n^9$  (C)  $n^7$  (E)  $n^5$  (G)  $n^3$  (I)  $n$

(B)  $n^8$  (D)  $n^6$  (F)  $n^4$  (H)  $n^2$  (J) 1

```
int main ( int argc, char * * argv ) {
    int n = atoi(argv[1]);
    if ( simpleCompare ) {
        f = n; do {
            e = n; do {
                b = 1; do {
                    c = n; while ( c > 1 ) {
                        if ( simpleCompare ) {
                            simpleStatement;
                        }
                        c--; }
                    b += 5; } while ( b < n );
                e -= 3; } while ( e > 1 );
            f--; } while ( f > 1 );
    } else {
        for ( h = n ; h > 1 ; h -= 1 ) {
            i = n; while ( i > 1 ) {
                j = n; do {
                    simpleStatement;
                } while ( j > 1 );
                i -= 10; }
        }
    }
    return 0; }
```

- 5/2p. Give a tight big-oh  $\Theta()$  bound on the running time  $T(n)$  of this program.  
Assume `atoi`, `simpleStatement`, and `simpleCompare` each run in  $\Theta(1)$  time.  
(A)  $n^9$  (C)  $n^7$  (E)  $n^5$  (G)  $n^3$  (I)  $n$   
(B)  $n^8$  (D)  $n^6$  (F)  $n^4$  (H)  $n^2$  (J) 1

```
int main ( int argc, char * * argv ) {
    int n = atoi(argv[1]);
    if ( simpleCompare ) {
        if ( simpleCompare ) {
            simpleStatement;
        } else {
            simpleStatement;
        }
    } else {
        simpleStatement;
    }
    return 0; }
```

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- 6/2p. Give a tight big-oh  $\Theta()$  bound on the running time  $T(n)$  of this program.  
Assume `atoi`, `simpleStatement`, and `simpleCompare` each run in  $\Theta(1)$  time.  
(A)  $n^9$  (C)  $n^7$  (E)  $n^5$  (G)  $n^3$  (I)  $n$   
(B)  $n^8$  (D)  $n^6$  (F)  $n^4$  (H)  $n^2$  (J) 1

```
int main ( int argc, char * * argv ) {
    int n = atoi(argv[1]);
    if ( simpleCompare ) {
        if ( simpleCompare ) {
            b = n; while ( b > 1 ) {
                if ( simpleCompare ) {
                    simpleStatement;
                } else {
                    simpleStatement;
                }
            }
            b--; }
        } else {
            if ( simpleCompare ) {
                simpleStatement;
            } else {
                simpleStatement;
            }
        }
    } else {
        f = n; while ( f > 1 ) {
            if ( simpleCompare ) {
                simpleStatement;
            }
            f--; }
    }
    return 0; }
```

7/2p. Give a tight big-oh  $\Theta()$  bound on the running time  $T(n)$  of this program.

Assume `atoi`, `simpleStatement`, and `simpleCompare` each run in  $\Theta(1)$  time.

(A)  $n^9$  (C)  $n^7$  (E)  $n^5$  (G)  $n^3$  (I)  $n$

(B)  $n^8$  (D)  $n^6$  (F)  $n^4$  (H)  $n^2$  (J) 1

```
int main ( int argc, char * * argv ) {
    int n = atoi(argv[1]);
    if ( simpleCompare ) {
        e = n; while ( e > 1 ) {
            a = n; while ( a > 1 ) {
                if ( simpleCompare ) {
                    for ( c = 1 ; c < n ; c += 3 ) {
                        if ( simpleCompare ) {
                            k = 1; while ( k < n ) {
                                simpleStatement;
                                k++; }
                        }
                    }
                }
            }
            a -= 5; }
        e--; }
    }
    return 0; }
```

8/2p. Give a tight big-oh  $\Theta()$  bound on the running time  $T(n)$  of this program.

Assume `atoi`, `simpleStatement`, and `simpleCompare` each run in  $\Theta(1)$  time.

(A)  $n^9$  (C)  $n^7$  (E)  $n^5$  (G)  $n^3$  (I)  $n$

(B)  $n^8$  (D)  $n^6$  (F)  $n^4$  (H)  $n^2$  (J) 1

```
int main ( int argc, char * * argv ) {
    int n = atoi(argv[1]);
    if ( simpleCompare ) {
        if ( simpleCompare ) {
            f = 1; while ( f < n ) {
                for ( d = n ; d > 1 ; d-- ) {
                    simpleStatement;
                }
                f++; }
        } else {
            simpleStatement;
        }
    } else {
        e = 1; while ( e < n ) {
            b = n; while ( b > 1 ) {
                simpleStatement;
                b--; }
            e += 3; }
    }
    return 0; }
```

9/2p. Give a tight big-oh  $\Theta()$  bound on the running time  $T(n)$  of this program.  
Assume `atoi`, `simpleStatement`, and `simpleCompare` each run in  $\Theta(1)$  time.

- (A)  $n^9$  (C)  $n^7$  (E)  $n^5$  (G)  $n^3$  (I)  $n$   
(B)  $n^8$  (D)  $n^6$  (F)  $n^4$  (H)  $n^2$  (J) 1

```
int main ( int argc, char * * argv ) {
    int n = atoi(argv[1]);
    if ( simpleCompare ) {
        for ( i = n ; i > 1 ; i -= 5 ) {
            if ( simpleCompare ) {
                e = n; do {
                    d = 1; do {
                        g = 1; do {
                            h = n; while ( h > 1 ) {
                                if ( simpleCompare ) {
                                    a = 1; do {
                                        simpleStatement;
                                        a++; } while ( a < n );
                                } else {
                                    simpleStatement;
                                }
                                h--; }
                            g += 10; } while ( g < n );
                        d++; } while ( d < n );
                    e--; } while ( e > 1 );
            } else {
                if ( simpleCompare ) {
                    if ( simpleCompare ) {
                        f = n; while ( f > 1 ) {
                            if ( simpleCompare ) {
                                simpleStatement;
                            }
                            f--; }
                    } else {
                        simpleStatement;
                    }
                } else {
                    if ( simpleCompare ) {
                        simpleStatement;
                    }
                }
            }
        }
    }
    return 0; }
```

- 10/2p. Give a tight big-oh  $\Theta()$  bound on the running time  $T(n)$  of this program.  
Assume `atoi`, `simpleStatement`, and `simpleCompare` each run in  $\Theta(1)$  time.  
(A)  $n^9$  (C)  $n^7$  (E)  $n^5$  (G)  $n^3$  (I)  $n$   
(B)  $n^8$  (D)  $n^6$  (F)  $n^4$  (H)  $n^2$  (J) 1

```
int main ( int argc, char * * argv ) {
    int n = atoi(argv[1]);
    if ( simpleCompare ) {
        e = n; while ( e > 1 ) {
            g = 1; while ( g < n ) {
                if ( simpleCompare ) {
                    if ( simpleCompare ) {
                        for ( a = n ; a > 1 ; a -= 2 ) {
                            for ( f = 1 ; f < n ; f += 3 ) {
                                if ( simpleCompare ) {
                                    if ( simpleCompare ) {
                                        for ( j = n ; j > 1 ; j-- ) {
                                            simpleStatement;
                                        }
                                    } else {
                                        simpleStatement;
                                    }
                                } else {
                                    if ( simpleCompare ) {
                                        simpleStatement;
                                    } else {
                                        simpleStatement;
                                    }
                                }
                            }
                        }
                    }
                }
            }
        } else {
            b = n; do {
                for ( k = n ; k > 1 ; k-- ) {
                    if ( simpleCompare ) {
                        if ( simpleCompare ) {
                            for ( d = 1 ; d < n ; d += 2 ) {
                                simpleStatement;
                            }
                        }
                    }
                }
            } while ( b > 1 );
            b--;
        }
        g++;
        e--;
    }
    return 0;
}
```

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Total points 20.

**Answer Key** (points per line)

1	(2).	G	( $n^3$ )
2	(2).	H	( $n^2$ )
3	(2).	I	( $n$ )
4	(2).	F	( $n^4$ )
5	(2).	J	(1)
6	(2).	I	( $n$ )
7	(2).	F	( $n^4$ )
8	(2).	H	( $n^2$ )
9	(2).	D	( $n^6$ )
10	(2).	E	( $n^5$ )

Total points 20.